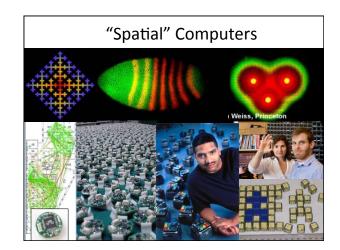
### Global-to-Local Theory CS289



### Why Global-to-local Theory?

- Global-to-local compilers allows us to transform a class of global goals into local rules for individual agents
  - Robustness, scalability, provable..
- But they do not tell us what is computable
  - · Local to Global is hard: e.g. Conway's Game of Life
  - But, Global to Local is possible: Yamins, PhD 2008

# Cellular Automata • Stanislaw Ulam and John von Neumann (1940s) - Simulate "discrete" biology & physics; - Self-replicating machines • Conway's Game of Life (1970s) - A simple intuitive rule....amazing dynamic patterns! - Turing Complete! (2002) • Wolfram, A New Kind of Science, 2002 - Systematic classification of all 1D two-state CA rules

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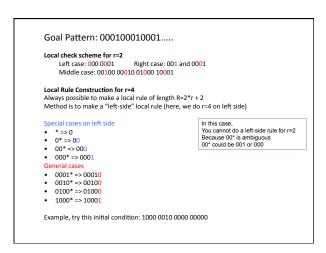
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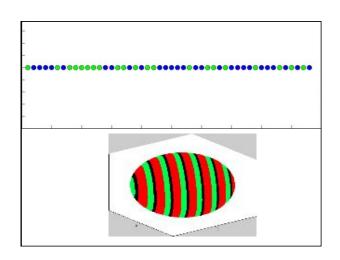
# The Setup • 1D multi-agent system (like cellular automata) LOCAL RULE n agent state m=R,B agent local view, r = 2

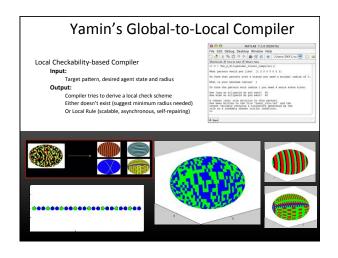
### The Setup • 1D multi-agent system (like cellular automata) LOCAL RULE n agents agent state m=R,B agent local view, r = 2 • Goal: Self-organize target pattern Scalable to more agents Any initial condition Any timing model

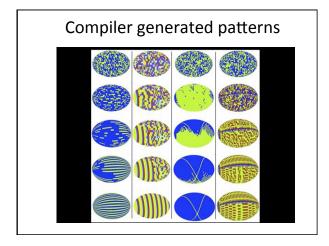
### Theoretical Underpinnings • Local Checkability — Given agent model (r, m) — Can you design a "voting" scheme such that if every agent says 1, then the global pattern is in goal space. — Necessary and Sufficient\* • If no check exists => no solution exists — Can use to to prove minimal requirements • If a check is available => — Can automatically produce a local rule, but with slightly larger radius (R=2r+2) — Provably correct, robust to asynchrony, self-repairing

### Lets do an example • Goal Pattern: 000100010001.....0001 1) Design and prove correct a local check scheme for r=2 2) Prove that no local check scheme can be designed for r=1 3) How would you add state (change pattern) to make r=1 possible? 4) Make a local rule of radius r=4 for the original pattern 5) Prove there is no local check of finite radius for the half-n-half pattern (0°1°) pattern



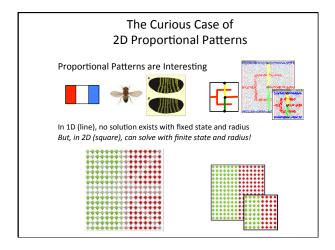






### Some Thoughts

- So far we have tackled 1D systems. Can we generalize the ideas to other agent models?
- Open Questions:
  - More complex patterns
    - E.g. Majority vote (Melanie Mitchell)
  - Approximate (high-probability) solutions
  - More complex spaces
    - 2D or 3D cellular automata
    - Agents moving in space (robots, dna self-assembly)



### **Theoretical Underpinnings**

- Reason theoretically about intuitive things
  - How one can tradeoff state and radius
  - Why some things are harder than others
  - Why some things take longer than others
  - How simple patterns can be combined to make complex ones
  - Why 1D patterns are like Strings (relation to grammars)
  - Why global-to-local is possible in CAs, whereas local-to-global may be so complex....