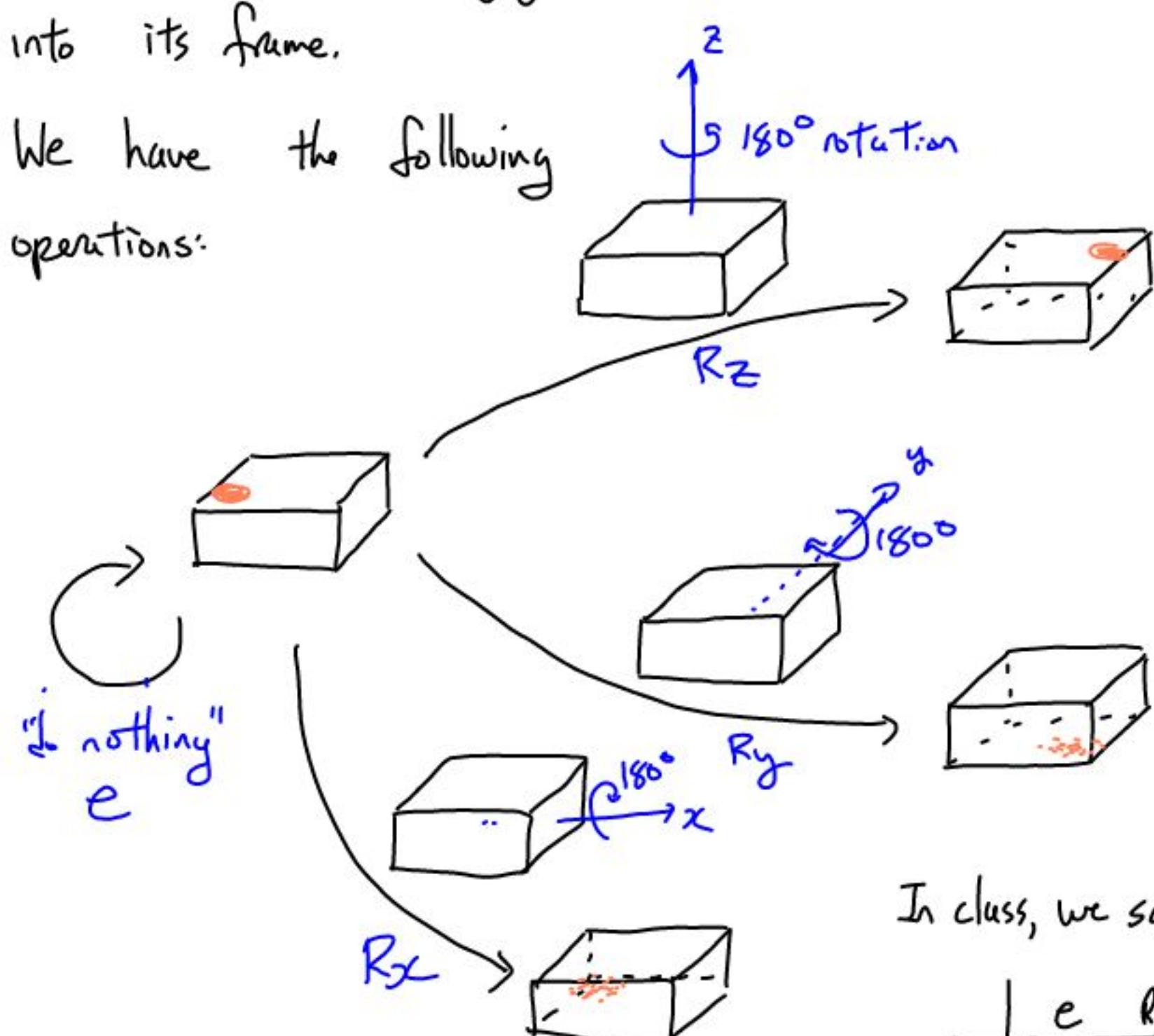


The Mattress Group!

Let M be a mattress.

("mattress" has not been rigorously defined in this class.) The mattress group is the group of symmetries of M — ie, the collection of things we can do to M while M still fits snugly into its frame.

We have the following operations:



In class, we saw:

	e	R_x	R_y	R_z
e	e	R_x	R_y	R_z
R_x	R_x	e	R_z	R_y
R_y	R_y	R_z	e	R_x
R_z	R_z	R_y	R_x	e

Some principles I stated:

(You can prove those if you want; they're not bad!)

- In a group's multiplication table, each row/column contains each element of G exactly once. (use cancellation law).
- If a mult. table is symmetric about diagonal, G is abelian.

$$\begin{array}{c|ccc} & h & \dots & g \\ \hline h & h^2 & & hg \\ \vdots & & & \\ g & gh & & g^2 \end{array}$$

$\Leftrightarrow gh = hg$.

diagonal

Example: Mattress group is abelian.